

88147301

**MATHEMATICS
STANDARD LEVEL
PAPER 1**

Candidate session number

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Wednesday 12 November 2014 (afternoon)

Examination code

1 hour 30 minutes

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INSTRUCTIONS TO CANDIDATES

- Write your session number in the boxes above.
- Do not open this examination paper until instructed to do so.
- You are not permitted access to any calculator for this paper.
- Section A: answer all questions in the boxes provided.
- Section B: answer all questions in the answer booklet provided. Fill in your session number on the front of the answer booklet, and attach it to this examination paper and your cover sheet using the tag provided.
- Unless otherwise stated in the question, all numerical answers should be given exactly or correct to three significant figures.
- A clean copy of the **Mathematics SL formula booklet** is required for this paper.
- The maximum mark for this examination paper is [90 marks].



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SECTION A

1. [*Maximum mark: 7*]

Let $f(x) = x^2 + x - 6$.

- (a) Write down the y -intercept of the graph of f . [1]
- (b) Solve $f(x) = 0$. [3]

[illegible]

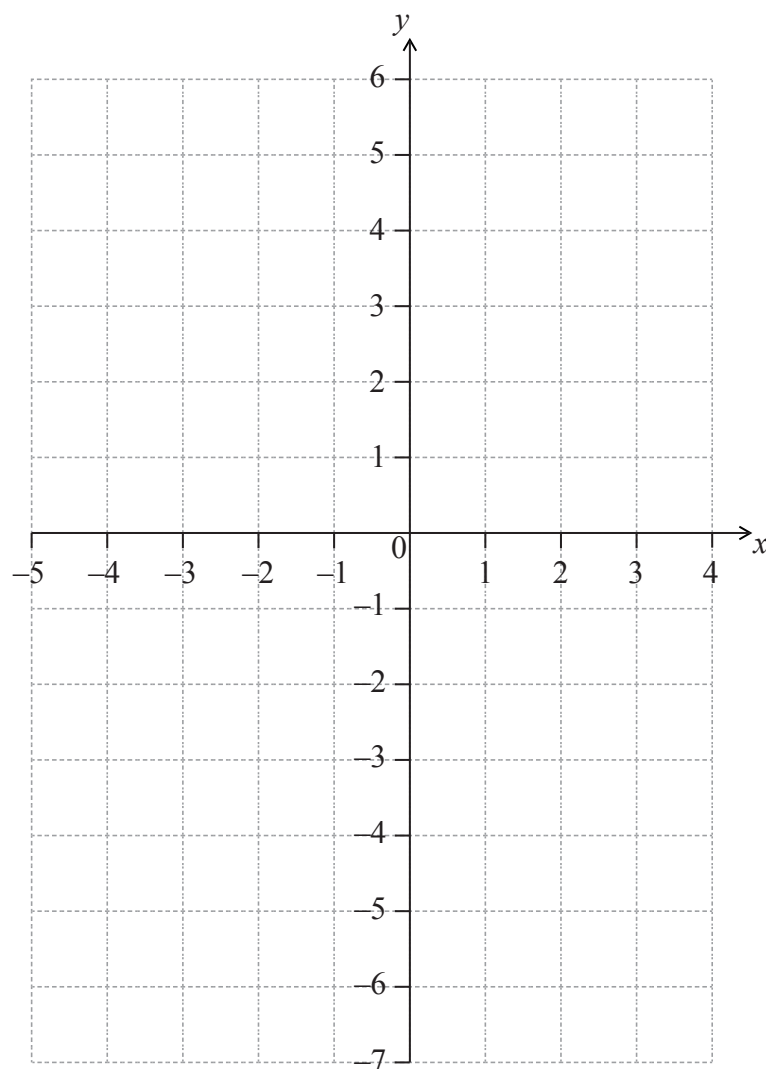
(This question continues on the following page)



(Question 1 continued)

(c) On the following grid, sketch the graph of f , for $-4 \leq x \leq 3$.

[3]



2. [Maximum mark: 6]

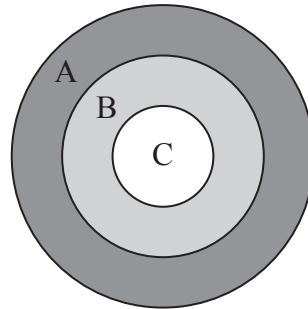
In an arithmetic sequence, the first term is 2 and the second term is 5.

- (a) Find the common difference. [2]
- (b) Find the eighth term. [2]
- (c) Find the sum of the first eight terms of the sequence. [2]



3. [Maximum mark: 7]

The following diagram shows a board which is divided into three regions A, B and C.



A game consists of a contestant throwing one dart at the board. The probability of hitting each region is given in the following table.

Region	A	B	C
Probability	$\frac{5}{20}$	$\frac{4}{20}$	$\frac{1}{20}$

(a) Find the probability that the dart does **not** hit the board.

[3]

The contestant scores points as shown in the following table.

Region	A	B	C	Does not hit the board
Points	0	q	10	–3

(b) Given that the game is fair, find the value of q .

[4]



4. [Maximum mark: 6]

(a) Write the expression $3\ln 2 - \ln 4$ in the form $\ln k$, where $k \in \mathbb{Z}$. [3]

(b) Hence or otherwise, solve $3\ln 2 - \ln 4 = -\ln x$. [3]

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5. [Maximum mark: 6]

Let $f(x) = p + \frac{9}{x-q}$, for $x \neq q$. The line $x = 3$ is a vertical asymptote to the graph of f .

- (a) Write down the value of q . [1]

The graph of f has a y -intercept at $(0, 4)$.

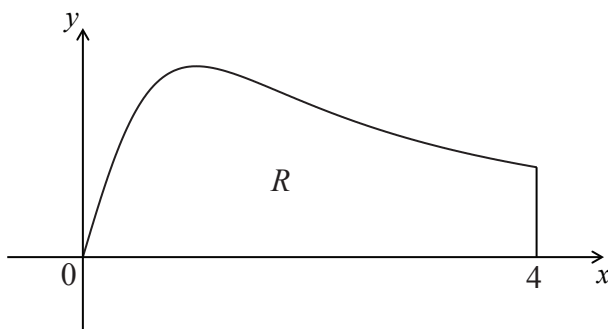
- (b) Find the value of p . [4]

- (c) Write down the equation of the horizontal asymptote of the graph of f . [1]

[illegible]

6. [Maximum mark: 6]

The following diagram shows the graph of $f(x) = \frac{x}{x^2 + 1}$, for $0 \leq x \leq 4$, and the line $x = 4$.



Let R be the region enclosed by the graph of f , the x -axis and the line $x = 4$.

Find the area of R .

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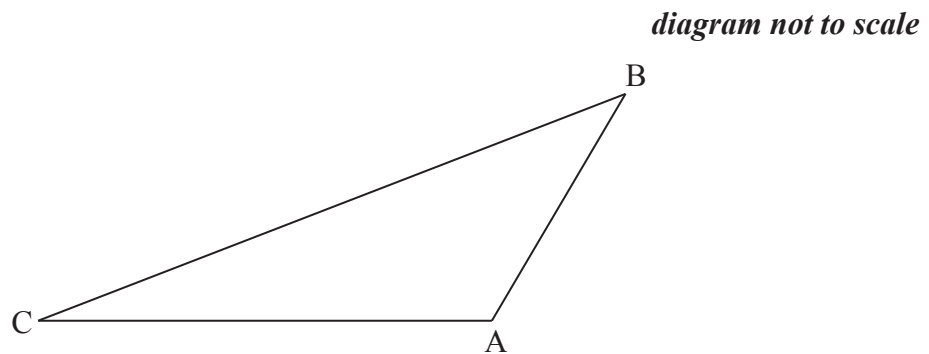
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7. [Maximum mark: 6]

The following diagram shows triangle ABC.



Let $\vec{AB} \cdot \vec{AC} = -5\sqrt{3}$ and $|\vec{AB}| |\vec{AC}| = 10$. Find the area of triangle ABC.

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SECTION B

Answer **all** questions in the answer booklet provided. Please start each question on a new page.

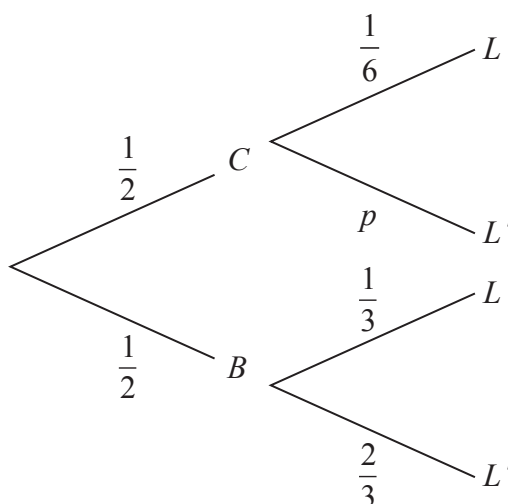
8. [Maximum mark: 15]

Adam travels to school by car (C) or by bicycle (B). On any particular day he is equally likely to travel by car or by bicycle.

The probability of being late (L) for school is $\frac{1}{6}$ if he travels by car.

The probability of being late for school is $\frac{1}{3}$ if he travels by bicycle.

This information is represented by the following tree diagram.



(a) Find the value of p . [2]

(b) Find the probability that Adam will travel by car and be late for school. [2]

(c) Find the probability that Adam will be late for school. [4]

(d) Given that Adam is late for school, find the probability that he travelled by car. [3]

Adam will go to school three times next week.

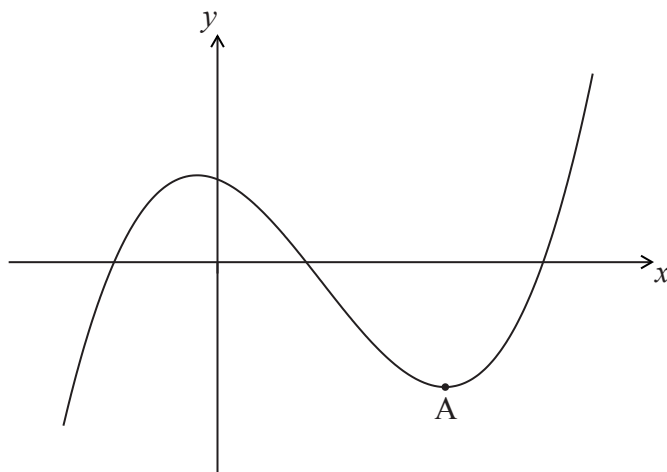
(e) Find the probability that Adam will be late exactly once. [4]



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9. [Maximum mark: 14]

The following diagram shows the graph of a function f . There is a local minimum point at A, where $x > 0$.



The derivative of f is given by $f'(x) = 3x^2 - 8x - 3$.

(a) Find the x -coordinate of A. [5]

(b) The y -intercept of the graph is at $(0, 6)$. Find an expression for $f(x)$. [6]

The graph of a function g is obtained by reflecting the graph of f in the y -axis, followed by a translation of $\begin{pmatrix} m \\ n \end{pmatrix}$.

(c) Find the x -coordinate of the local minimum point on the graph of g . [3]



Do **NOT** write solutions on this page.

10. [Maximum mark: 17]

Let L_x be a family of lines with equation given by $\mathbf{r} = \begin{pmatrix} x \\ 2 \\ x \end{pmatrix} + t \begin{pmatrix} x^2 \\ -2 \end{pmatrix}$, where $x > 0$.

(a) Write down the equation of L_1 . [2]

A line L_a crosses the y -axis at a point P.

(b) Show that P has coordinates $\left(0, \frac{4}{a}\right)$. [6]

The line L_a crosses the x -axis at $Q(2a, 0)$. Let $d = PQ^2$.

(c) Show that $d = 4a^2 + \frac{16}{a^2}$. [2]

(d) There is a minimum value for d . Find the value of a that gives this minimum value. [7]

