

Name:

Exam Style Questions

Arithmetic Progressions



Equipment needed: Pen and Calculator

### Guidance

1. Read each question carefully before you begin answering it.
2. Check your answers seem right.
3. Always show your workings

Video Tutorial

[www.corbettmaths.com/contents](http://www.corbettmaths.com/contents)

Video 374



Answers and Video Solutions



1. Here are the first four terms of a sequence



$$\begin{array}{cccc} 17 & 21 & 25 & 29 \\ +4 & +4 & +4 & +4 \end{array}$$

(a) Work out the next term in the sequence

33

(1)

(b) Explain how you worked out the answer to part (a).

The common difference is 4, so to find the next term, add 4 to 29.

(1)

2. The first two terms of an arithmetic progression are 6 and 12



Work out the next term.

$$\begin{array}{ccc} 6 & 12 & 18 \\ +6 & +6 & \end{array}$$

18

(1)

3. An arithmetic progression begins -2, 8, ...



Work out the next three terms.

$$\begin{array}{cccccc} -2 & 8 & 18 & 28 & 38 \\ +10 & +10 & +10 & +10 & \end{array}$$

18 28 38

(2)

4. Which of the following is an arithmetic progression?



Circle the correct answer.

3 6 12 24

3 6 9 15

3 4 6 9

3 5 7 9  
 $+2 +2 +2$

(1)

5. Which of the following is an arithmetic progression?



Circle the correct answer.

32 16 8 4

32 30 26 20

32 25 18 11  
 $-7 -7 -7$

32 8 2 0.5

(1)

6. Here are the first five terms of an arithmetic sequence.



9

13

17

21

25

Is 68 a term in the sequence?

Explain your answer.

No, 68 is even but all the terms  
in the sequence are odd.

(1)

7. Edwin has the following number cards.



Edwin chooses 3 of the number cards to make an arithmetic progression.

Write down 3 possible number cards that he could choose.

e.g.  $\boxed{6}$   $\boxed{13}$   $\boxed{20}$   
 e.g.  $13$   ~~$17$~~   $17$   $21$  <sup>(2)</sup>

8. Here are the first four terms of an arithmetic sequence.



2                      7                      12                      17

Find an expression, in terms of  $n$ , for the  $n$ th term of this sequence.

                    2      7      12      17  
 $s_n$       5      10      15      20

$$\frac{s_n - 3}{\dots\dots\dots}$$

(2)

9. Here are the first four terms of an arithmetic sequence.



-14                      -3                      8                      19

Find an expression, in terms of  $n$ , for the  $n$ th term of this sequence.

                    -14      -3      8      19  
 $11n$       11      22      33      44

$$\frac{11n - 25}{\dots\dots\dots}$$

(2)

10. Here are the first four terms of an arithmetic sequence.



7                      1                      -5                      -11

Find an expression, in terms of  $n$ , for the  $n$ th term of this sequence.

	7	1	-5	-11	
$-6n$	-6	-12	-18	-24	
					$-6n + 13$
					(2)

11. Here are the first four terms of an arithmetic sequence.



27                      34                      41                      48

(a) Find an expression, in terms of  $n$ , for the  $n$ th term of this sequence.

27	34	41	48	
7	14	21	28	
				$7n + 20$
				(2)

(b) Work out the 20th term in the sequence.

$$7 \times 20 + 20 = 160$$

$160$
(1)

(c) Show 380 is not a term in the sequence.

$$7n + 20 = 380$$

$$7n = 360$$

$$n = 51.428\dots$$

since  $51.428\dots$  is not a whole number,  
380 is not in the sequence.

(2)

12. The first two terms of an arithmetic progression are:



$$5k \xrightarrow{+5k} 10k \xrightarrow{+5k} 15k$$

Write down the next term.

15k

(1)

13. Yasmin attended a four year college course.



At the end of each of the 4 years, the students on the course sit an examination. The number of marks that each examination is worth, over the 4 years, form an arithmetic progression.

The examination at the end of the 1st year was worth 75 marks.

The examination at the end of the 2nd year was worth 110 marks.

In order to pass the course, a student needs to obtain at least 60% of the total available marks over the four years.

Yasmin scored a total of 309 marks.

Did Yasmin pass the course?

$$75 + 110 + 145 + 180 = 510$$

$$60\% \text{ of } 510 = 306 \quad (\text{since } 510 \times 0.6 = 306)$$

$$\text{Yes } 309 > 306$$

(5)

14. The first three terms of an arithmetic sequence are



$2a + b$

$3a + 6b$

$4a + 11b$

$5a + 16b$

Write down the next term in the sequence

$5a + 16b$

(1)

15. The first three terms of an arithmetic sequence are



$2k - 1$

$5k + 2$

$8k + 5$

Find, in terms of  $k$ , the 10th term of the sequence.

$2k - 1 \quad 5k + 2 \quad 8k + 5 \quad 11k + 8 \quad 14k + 11$

$17k + 14 \quad 20k + 17 \quad 23k + 20 \quad 26k + 23 \quad 29k + 26$

or

$$\begin{array}{cccc} 2 & 5 & 8 & \\ 3n-1 & 3 & 6 & 9 \end{array}$$

$$\begin{array}{cccc} & -1 & 2 & 5 \\ 3n-4 & 3 & 6 & 9 \end{array}$$

$3(10) - 1 = 29$

$29k$

$3(10) - 4 = 26$

$+ 26$

$29k + 26$

(4)

16. The first three terms of an arithmetic sequence are



$$2k \quad +9k \quad 11k \quad +9k \quad 20k$$

The sum of the first six terms of the sequence is 1029

Work out the value of  $k$ .

$$2k + 11k + 20k + 29k + 38k + 47k = 147k$$

$$147k = 1029$$

$$k = 7$$

7

.....  
(4)

17. The first three terms of an arithmetic sequence are



$x + 16$

$5x - 1$

$2x + 38$

Work out the value of  $x$ .

$$(5x - 1) - (x + 16) = (2x + 38) - (5x - 1)$$

$$4x - 17 = -3x + 39$$

$$7x = 56$$

$$x = 8$$

8

.....  
(4)