

Name:

Exam Style Questions

Circle Theorems



Corbettmaths

Equipment needed: Calculator, pen

Guidance

1. Read each question carefully before you begin answering it.
2. Check your answers seem right.
3. Always show your workings

Video Tutorial

www.corbettmaths.com/contents

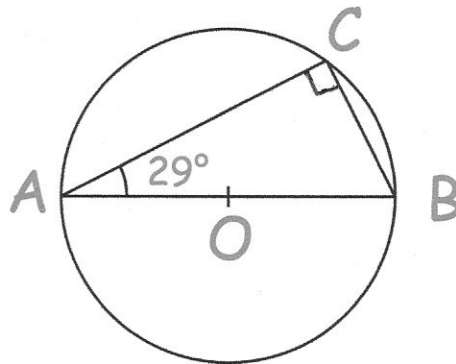
Videos 64, 65



Answers and Video Solutions



1. (a) In the diagram below, O is the centre of the circle and A, B and C are points on the circumference.



Angle A = 29°

Work out the size of angle B.

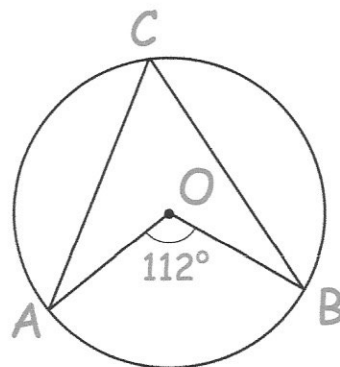
$$90 + 29 = 119$$

$$180 - 119 = 61$$

$$\dots\dots\dots 61^\circ$$

(1)

- (b) A, B and C are three points on the circumference of another circle. O is the centre of the circle.



Angle AOB = 112°

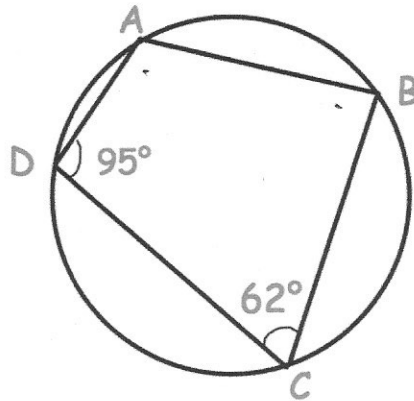
Work out the size of angle ACB.

$$112 \div 2 = 56$$

$$\dots\dots\dots 56^\circ$$

(1)

2. A, B, C and D are points on the circumference on a circle.



- (a) Find the size of angle DAB.

$$180 - 62 = 118^\circ$$

$$\begin{array}{r} 118 \\ \hline \end{array}^\circ$$

(1)

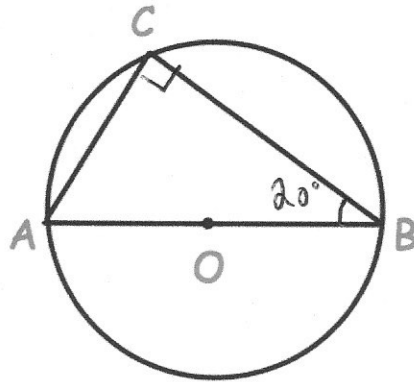
- (b) Find the size of angle ABC.

$$180 - 95 = 85$$

$$\begin{array}{r} 85 \\ \hline \end{array}^\circ$$

(1)

3. A circle with centre O, has points A, B and C on the circumference.
Angle ABC = 20°



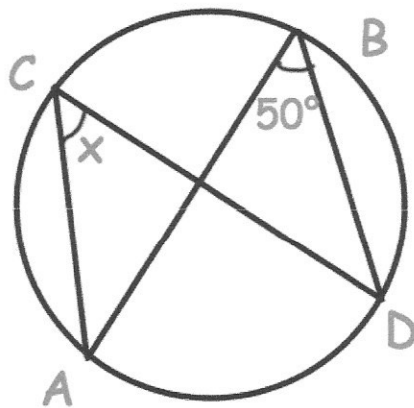
Find the size of angle BAC.

$$90 + 20 = 110$$

$$180 - 110 = 70$$

.....^o
70
(1)

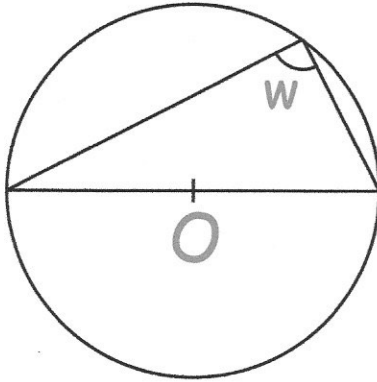
4. A, B, C and D are points on the circumference of a circle.



Find x, the size of angle ACD.

.....^o
50
(1)

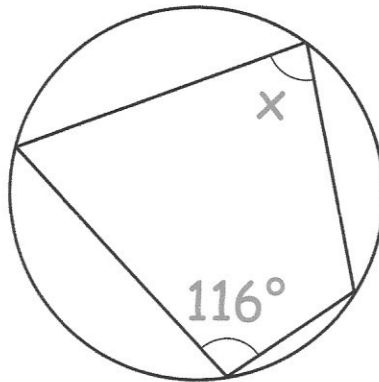
5. (a) In the diagram, O is the centre of the circle.



Write down the value of w.

90
.....°
(1)

- (b)

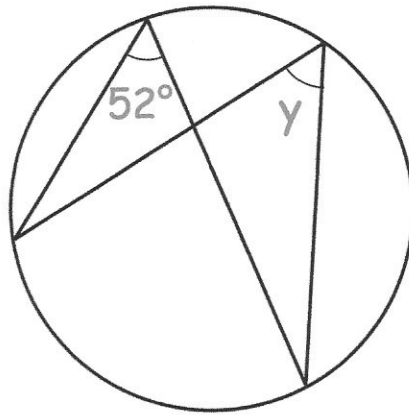


Write down the value of x.

$$180 - 116 = 64$$

64
.....°
(1)

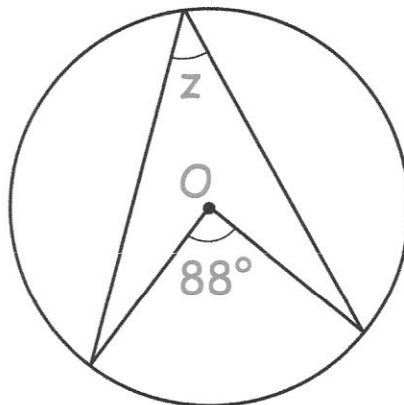
(c)



Write down the value of y .

52
.....^o
(1)

(d) In the diagram, O is the centre of the circle.

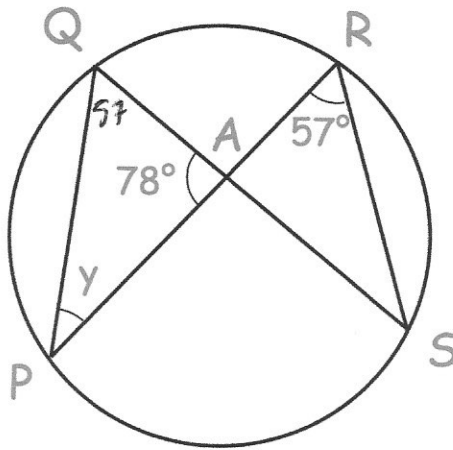


Write down the value of z .

$$88 \div 2 = 44$$

44
.....^o
(1)

6. P, Q, R and S are four points on the circumference of a circle.
 PR meets QS at A.
 Angle PRS = 57° and Angle PAQ = 78°



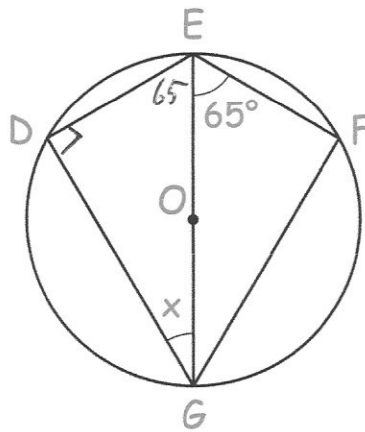
Work out the value of angle y .
 Include your method.

$$78 + 57 = 135$$

$$180 - 135 = 45$$

.....
 45°
 (3)

7. The diagram shows points D, E, F and G on the circumference of a circle.
 EG is a diameter.
 DEFG is a kite.



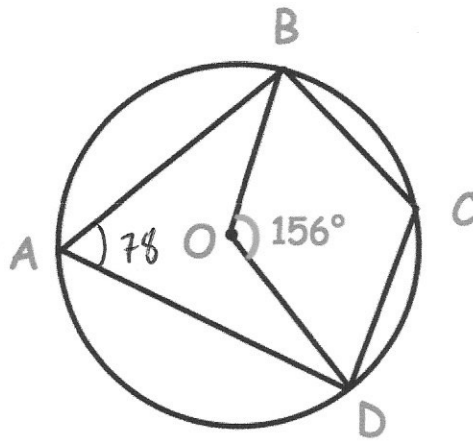
Work out the value of x .

$$90 + 65 = 155$$

$$180 - 155$$

.....
 25°
 (2)

8. A, B, C and D are points on the circumference of a circle with centre O.



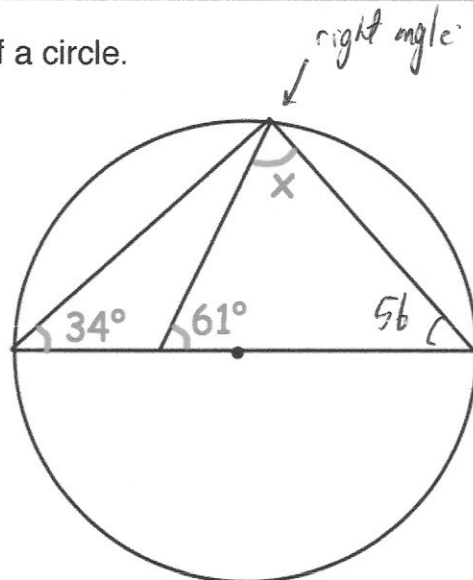
Work out the size of angle BCD.
You must show your workings.

$$156 \div 2 = 78$$

$$180 - 78 = 102$$

..... 102 °
(4)

9. AB is the diameter of a circle.



Work out the value of x.

$$90 + 34 = 124$$

$$180 - 124 = 56$$

$$56 + 61 = 117$$

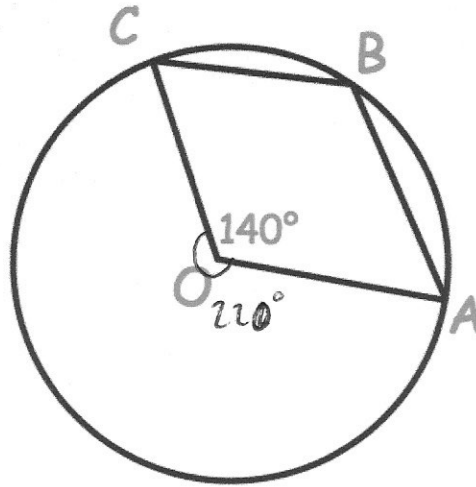
$$180 - 117 = 63$$

..... 63 °
(3)

10. The diagram shows a circle, centre O.
A, B and C are points on the circumference of the circle.



Angle AOC is 140°



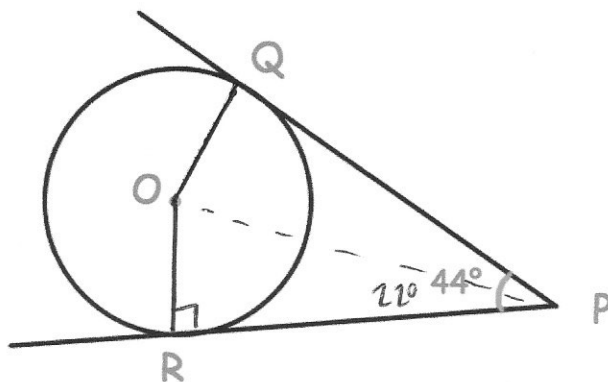
Explain why angle ABC is 110°

Reflex angle AOC = 220° , since $360 - 140 = 220^\circ$
as angles at a point add to 360° .

Angle ABC is half reflex angle AOC, $220 \div 2 = 110^\circ$

(2)

11. Q and R are points on a circle, centre O.
PQ and PR are tangents to the circle.



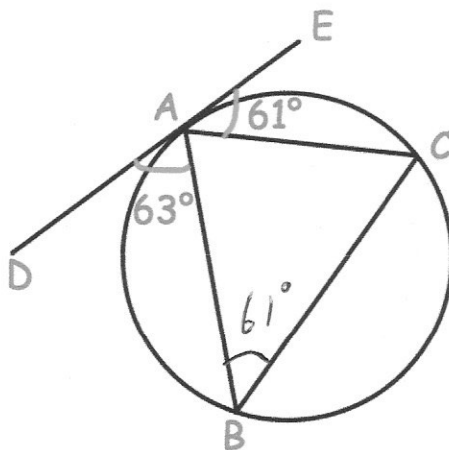
Work out the size of angle POR.

$$90 + 22 = 112$$

$$180 - 112 = 68$$

.....°
(3)

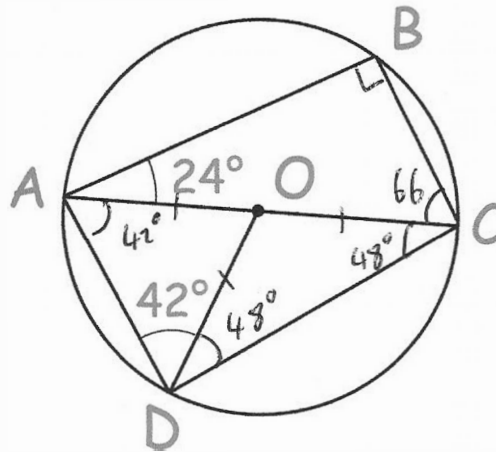
- 12.



DAE is a tangent to a circle.
Write down the size of angle ABC.

.....°
(1)

13.



In the diagram O is the centre of the circle.
 AOC is a straight line.
 Angle BAO is 24° and Angle ADO is 42°

(a) Find the size of angle CAD.

42

 (1)

(b) Find the size of angle ACB.

$$24 + 90 = 114$$

$$180 - 114 = 66^\circ$$

66

 (1)

(c) Find the size of angle BCD.

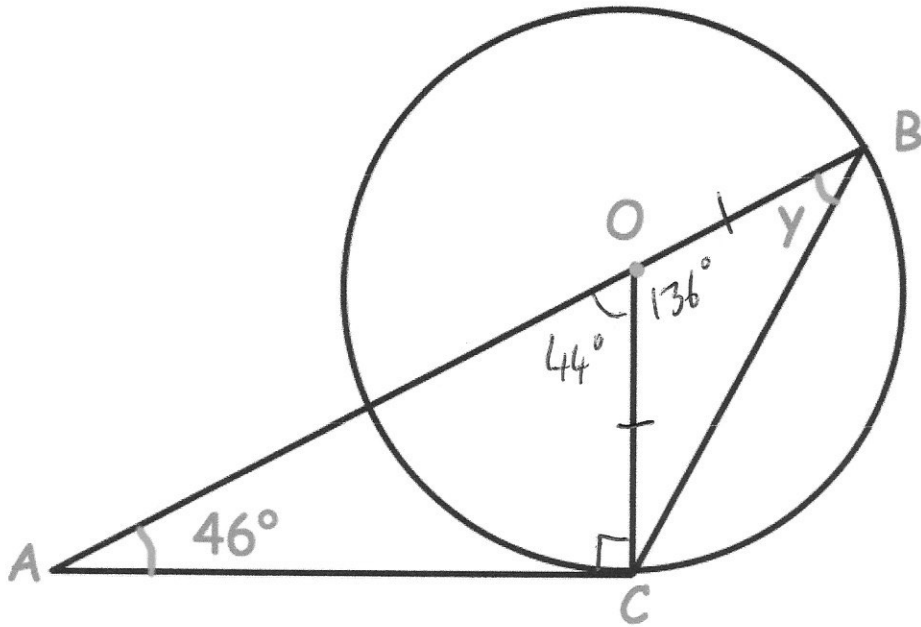
$$42 + 24 = 66^\circ$$

$$180 - 66 = 114$$

114

 (1)

14.



AOB is a straight line.

B and C are points on the circumference of a circle, centre O.

AC is a tangent to the circle.

Work out the size of the angle y.

$$90 + 46 = 136$$

$$180 - 136 = 44^\circ$$

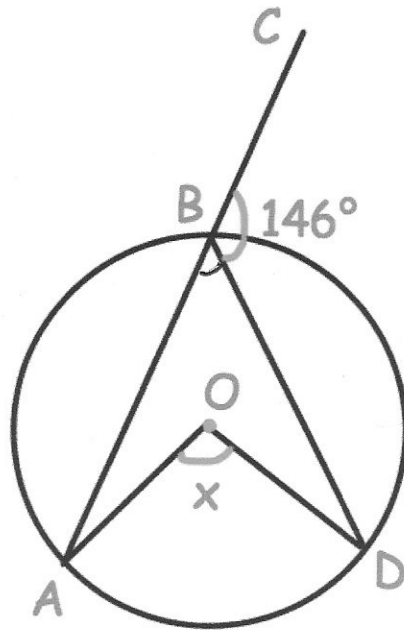
$$180 - 44 = 136$$

$$180 - 136 = 44$$

$$44 \div 2 = 22$$

.....
22°
(4)

15.



Shown is a circle with centre O.
ABC is a straight line.
Angle CBD is 146°

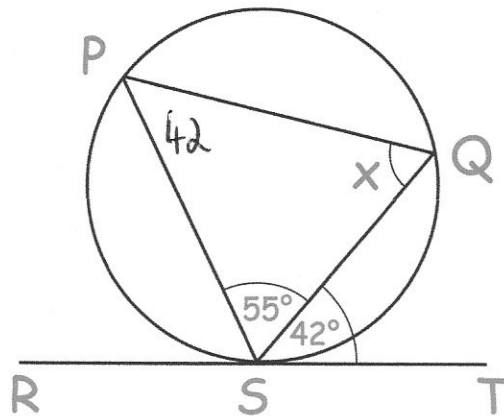
Find the size of angle AOD.

$$180 - 146 = 34$$

$$34 \times 2 = 68$$

.....^o
68
(3)

16. RT is a tangent to the circle at S.



$$42 + 55 = 97$$

$$180 - 97 = 83^\circ$$

Calculate the value of x .

Give reasons for your answer.

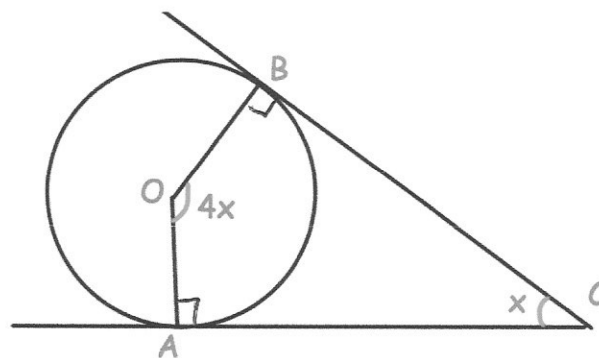
$$\angle SPQ = 42^\circ \quad (\text{Alternate segment theorem})$$

$$\angle PQS = 83^\circ \quad (\text{Angles in a triangle add to } 180^\circ)$$

83

.....^o
(3)

17. AC and BC are tangents to the circle with centre O.



Find the size of x .

$$4x + x + 90 + 90 = 360$$

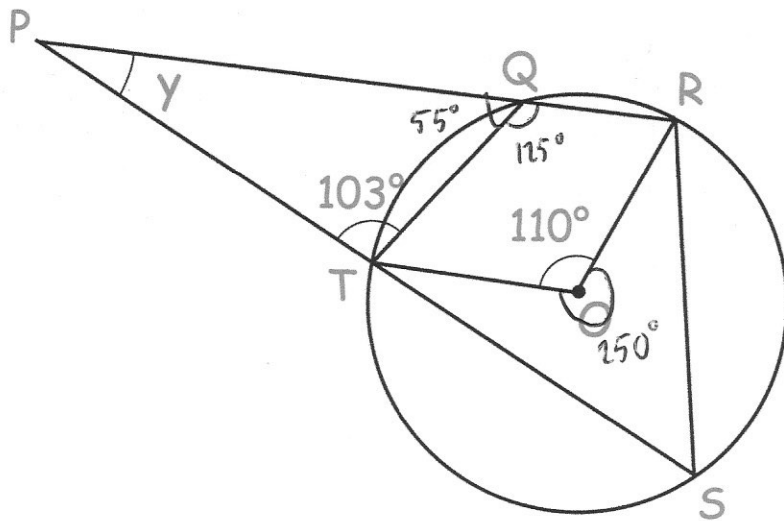
$$5x + 180 = 360$$

$$5x = 180$$

$$x = 36$$

.....36.....^o
(3)

18. Q, R, S and T are points on the circumference of a circle, centre O.



$$\begin{aligned}
 360 - 110 &= 250 \\
 250 \div 2 &= 125 \\
 180 - 125 &= 55 \\
 103 + 55 &= 158 \\
 180 - 158 &= 22^\circ
 \end{aligned}$$

PQR and PTS are both straight lines.

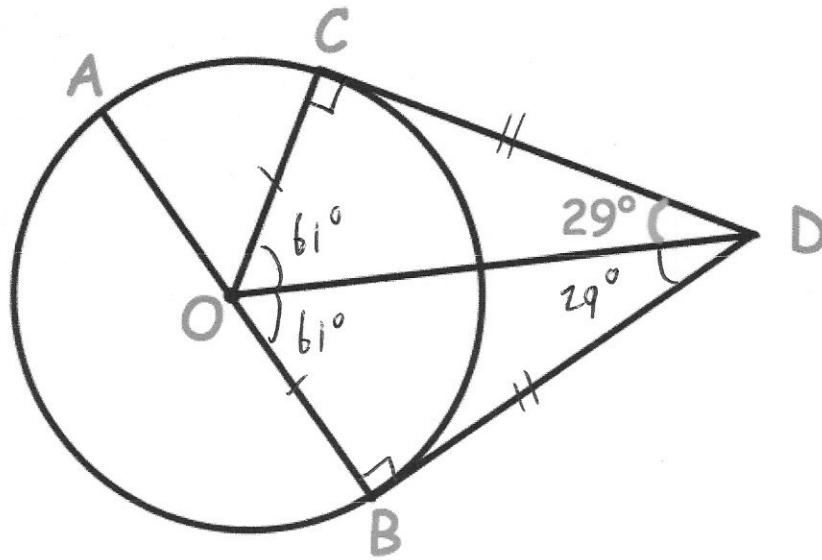
Find the size of angle RPS.

You must show all of your working.

$\text{Reflex } \angle ROT = 250^\circ$ as the angles at a point add to 360°
 $\angle RQT = 125^\circ$ angle at centre is twice angle at circumference.
 $\angle PQT = 55^\circ$ angles in a straight line add to 180° .
 $\angle RPS = 22^\circ$ angles in a triangle add to 180°

$\underline{\hspace{2cm} 22 \hspace{2cm}}^\circ$
 (3)

19. A, B and C are points on the circumference of a circle with centre O.



AOB is a diameter of the circle.
 CD and BD are tangents to the circle.
 Angle CDO = 29°

Work out the size of angle AOC.
 Give reasons for each stage of your working.

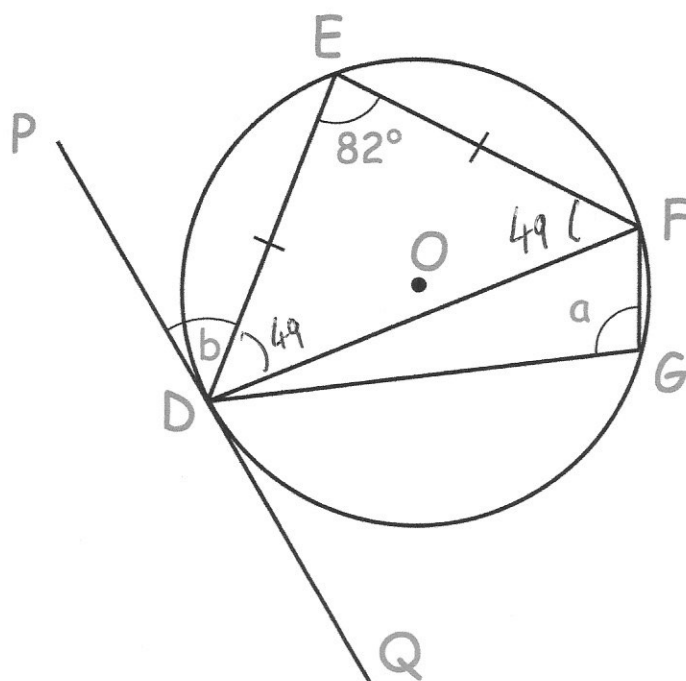
$CO = BO$ as tangents to a circle are equal length.
 $OC = OB$ both radii

$\therefore \angle COB = \angle BOD = 29^\circ$ as a kite has a line of symmetry.
 $\angle OCD = \angle OBD = 90^\circ$ tangent and radius meet at 90° .

$\angle COC = \angle BOB = 61^\circ$ angles in a triangle add to 180° .
 $\angle AOC = 180 - 61 - 61 = 58^\circ$ angles in a straight line add to 180° .

58[°]
 (4)

20. DEFG is a cyclic quadrilateral.
 PDQ is a tangent at D.
 O is the centre of the circle.
 DEF is an isosceles triangle.



- (a) Work out the value of a.

$$180 - 82 = 98$$

$$\frac{98}{2} = 49^\circ$$

(2)

- (b) Work out the value of b.

$$180 - 82 = 98$$

$$98 \div 2 = 49^\circ$$

$$\frac{98}{2} = 49^\circ$$

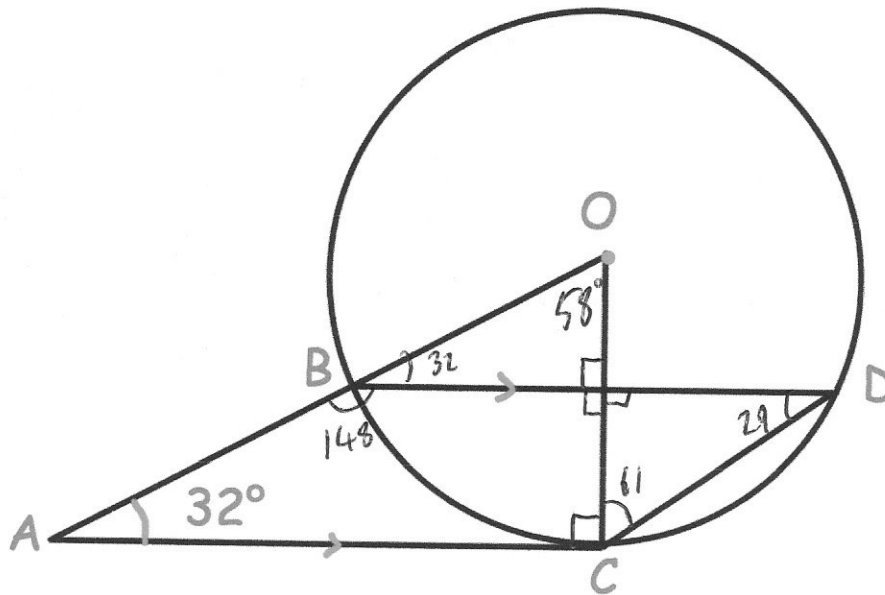
(3)

- (c) Write down the name of the circle theorem used in part (b)

Alternate segment theorem.

(1)

21.



Shown is a circle, centre O.
B, C and D are points on the circumference.

ABO is a straight line.
AC is a tangent to the circle.

(a) Work out angle AOC.

$$90 + 32 = 122$$

$$180 - 122 = 58^\circ$$

$$\begin{array}{r} 58 \\ \hline \end{array}^\circ$$

(2)

(b) Work out angle BDC.

$$58 \div 2 = 29$$

$$\begin{array}{r} 29 \\ \hline \end{array}^\circ$$

(3)

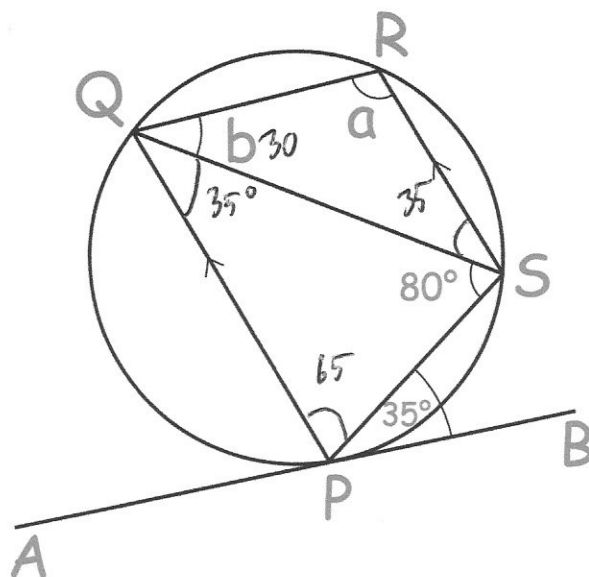
(c) Work out angle ACD.

$$90 + 61 = 151$$

$$\begin{array}{r} 151 \\ \hline \end{array}^\circ$$

(1)

22. PQRS is a cyclic quadrilateral.
 APB is a tangent to the circle at P.
 PQ is parallel to SR.
 Angle SPB = 35° and angle PSQ = 80°



- (a) Work out the size of angle QRS.

$$180 - 65 = 115$$

$$\begin{array}{r} 115 \\ \hline \end{array} \text{ }^\circ$$

(4)

- (b) Work out the size of angle RQS.

$$180 - 115 = 65^\circ$$

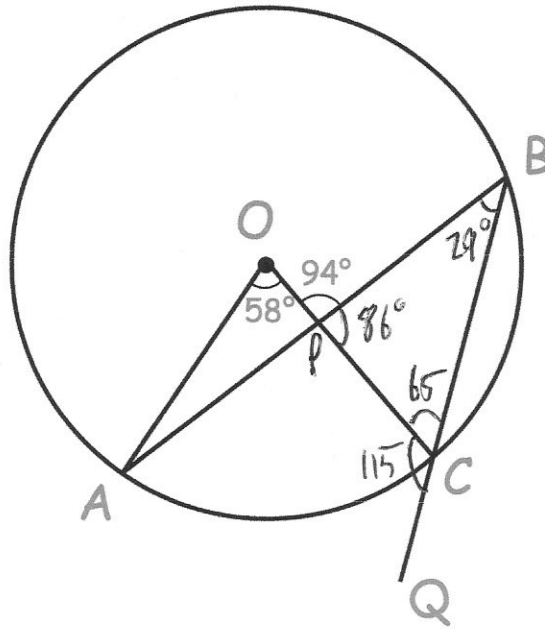
$$65 - 35 = 30$$

$$\begin{array}{r} \cancel{115} \quad 30 \\ \hline \end{array} \text{ }^\circ$$

(2)

180 - 115 = 65
65 - 35 = 30

23.



A, B and C are points on the circumference of a circle, centre O.

BCQ is a straight line.

Work out the size of angle OCQ.

Clearly explain each step of your solution.

$\angle ABC = 29^\circ$ angle at circumference is half the size of the angle at the centre.

$\angle BPC = 86^\circ$ angles in a straight line add to 180°

$\angle OCB = 65^\circ$ angles in a triangle add to 180°

$\angle OCQ = 115^\circ$ angles in a straight line add to 180°

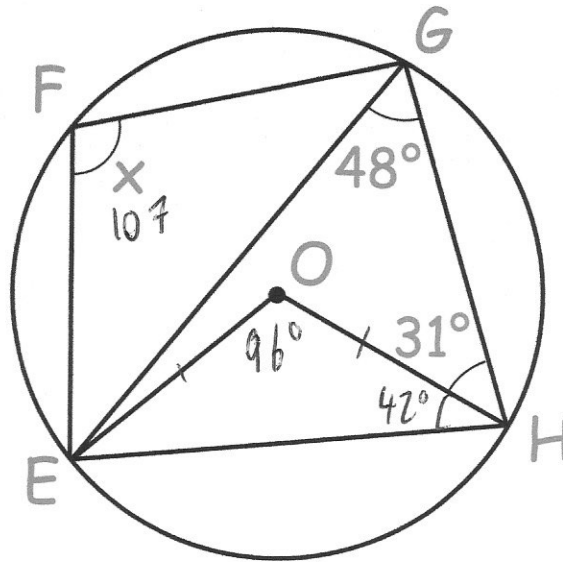
115
 $\dots\dots\dots^\circ$
(4)

24. E, F, G and H are points on the circumference of a circle with centre O.



Angle OHG = 31°

Angle EGH = 48°



Work out the size of angle EFG.

Give a reason for each stage of your working.

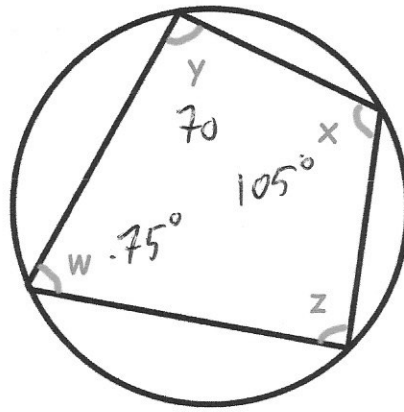
$\angle EOR = 96^\circ$ angle at centre is twice the angle at the circumference.

$\angle OHE = 42^\circ$ $\triangle OEH$ is isosceles and $\angle OEH = \angle OHE$.

$\angle GHE = 73^\circ$ $\angle OEG + \angle OHE$

$\angle EFG = 107^\circ$ opposite angles of cyclic quadrilaterals add to 180° .

.....107.....
(4)



$$w : x = 5 : 7$$

$$x : y = 3 : 2$$

Work out the size of angle z .

w & x add to 180° .

$$5 + 7 = 12$$

$$180 \div 12 = 15$$

$$5 \times 15 = 75^\circ$$

$$7 \times 15 = 105^\circ$$

$$105 \div 3 = 35$$

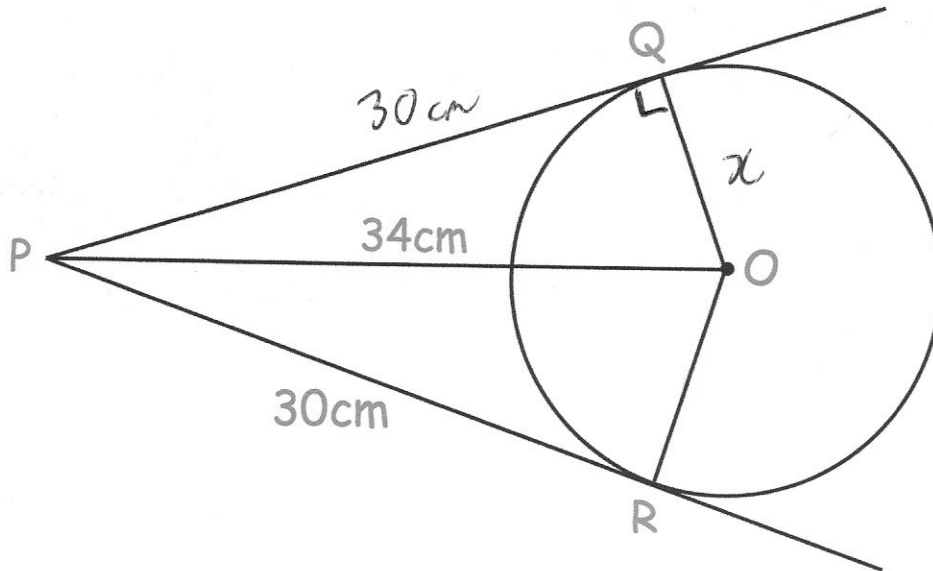
$$35 \times 2 = 70$$

$$180 - 70$$

$$z = \underline{110}^\circ$$

(5)

26.



Q and R are points on the circumference of a circle with centre O.

PQ and PR are tangents to the circle.

PR = 30cm

OP = 34cm

(a) Calculate the length of OQ.

$$30^2 + x^2 = 34^2$$

$$900 + x^2 = 1156$$

$$x^2 = 256$$

$$x = 16$$

16 cm
(3)

(b) Calculate the circumference of the circle.
Give your answer to 1 decimal place.

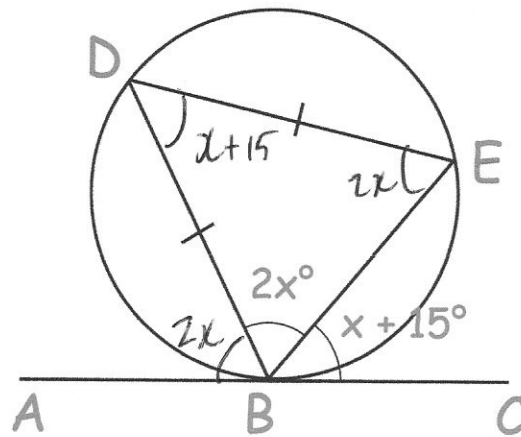
$$C = \pi \times d$$

$$= \pi \times 32$$

$$= 100.530\dots$$

100.5 cm
(2)

27.



B, D and E are points on the circumference of a circle.
AC is a tangent to the circle at point B.

Angle DBE = $2x^\circ$ Angle CBE = $x + 15^\circ$

Work out the size of angle ABD.

$$(x + 15) + 2x + 2x = 180$$

$$5x + 15 = 180$$

$$5x = 165$$

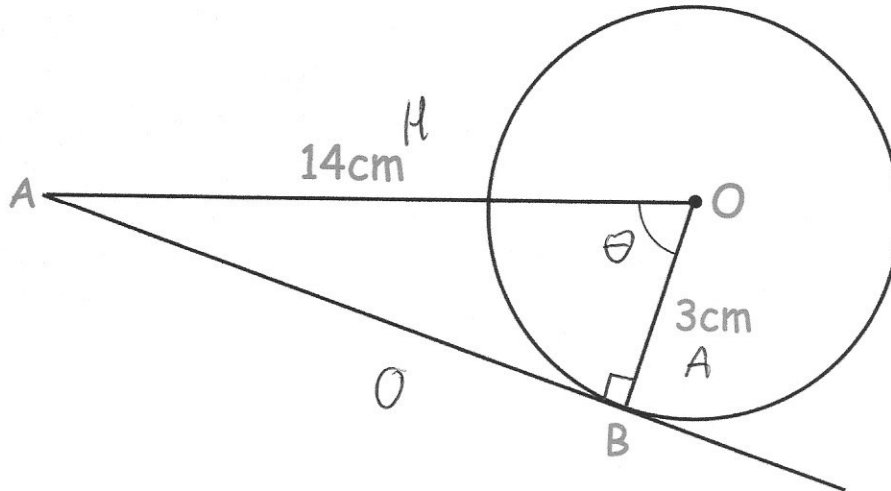
$$x = 33$$

$$2 \times 33 = 66^\circ$$

66

.....
(5)

28.



B is a point on the circumference of a circle with centre O.

AB is a tangent to the circle.

OA = 14cm and OB = 3cm

Calculate the size of angle AOB.

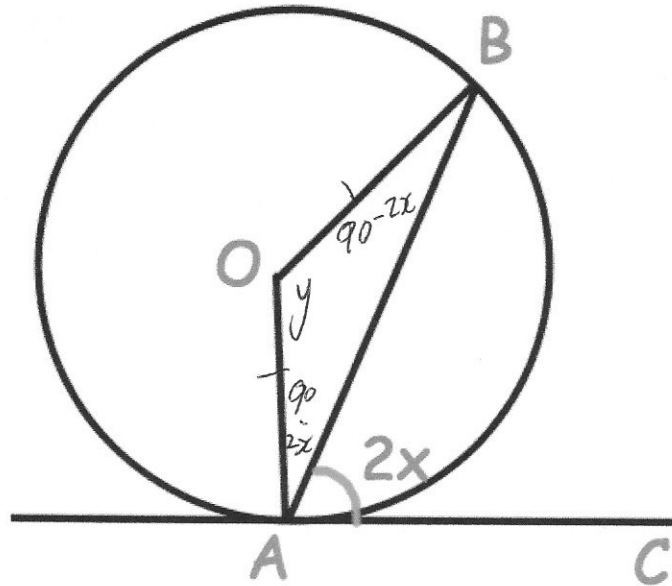
$$\cos \theta = \frac{3}{14}$$

$$\theta = \cos^{-1}\left(\frac{3}{14}\right)$$

$$= 77.62637\dots$$

$$\underline{\underline{77.63^\circ}} \quad (3)$$

29.



A and B are points on the circumference of a circle, centre O.
 CA is a tangent to the circle.
 Angle $CAB = 2x$

Prove that angle $AOB = 4x$
 Give reasons for each stage of your working.

$$\angle OAC = 90^\circ \quad \text{Angle between radius \& tangent is } 90^\circ.$$

$$\therefore \angle OAB = 90 - 2x$$

$\triangle OAB$ is isosceles.

$$\therefore \angle OBA = 90 - 2x$$

$$\angle OBA + \angle OAB + \angle AOB = 180^\circ \quad \text{Angles in a triangle add to } 180^\circ.$$

$$(90 - 2x) + (90 - 2x) + y = 180^\circ$$

$$180 + y - 4x = 180$$

$$y = 4x$$

$$\angle AOB = 4x$$

QED

(4)