

Name:

Exam Style Questions

# Equating Coefficients



Equipment needed: Pen

## Guidance

1. Read each question carefully before you begin answering it.
2. Check your answers seem right.
3. Always show your workings

Video Tutorial

[www.corbettmaths.com/contents](http://www.corbettmaths.com/contents)

Video 367



Answers and Video Solutions



1.

$$5(3x + c) \equiv 15x + 40$$

Work out the value of  $c$ .

$$15x + 5c \equiv 15x + 40$$

Constants

$$5c = 40$$

$$c = 8$$

$$c = \dots 8 \dots$$

(1)

2.

Work out the values of  $c$  and  $d$  in the identity.

$$2(x + 7) + cx + d \equiv 5x + 1$$

$$2x + 14 + cx + d \equiv 5x + 1$$

$x$

$$2 + c = 5$$

$$c = 3$$

Constants

$$14 + d = 1$$

$$d = -13$$

$$c = \dots 3 \dots$$

$$d = \dots -13 \dots$$

(3)

3.

$$a(2x + 7) \equiv 8x + 14b$$



Work out the values of a and b.

$$2ax + 7a \equiv 8x + 14b$$

 $x$ 

$$2a = 8$$

$$a = 4$$

 $(\text{Constants})$ 

$$7a = 14b$$

$$28 = 14b$$

$$b = 2$$

$$a = \overset{4}{\dots\dots\dots}$$

$$b = \overset{\cancel{2}}{2}{\dots\dots\dots}$$

(3)

4.

Work out the values of c and d in the identity.



$$(c - 2)x^2 + 3d \equiv 7x^2 + 9$$

$$cx^2 - 2x^2 + 3d \equiv 7x^2 + 9$$

 $x^2$ 

$$c - 2 = 7$$

$$c = 9$$

 $(\text{Constants})$ 

$$3d = 9$$

$$d = 3$$

$$c = \overset{9}{\dots\dots\dots}$$

$$d = \overset{3}{\dots\dots\dots}$$

(2)

5. Work out the values of a and b in the identity.



$$9(2x + 5) + 2(3x + b) \equiv ax + 23$$

$$18x + 45 + 6x + 2b \equiv ax + 23$$

(x)  $18 + 6 = a$

$$24 = a$$

(Constants)

$$45 + 2b = 23$$

$$2b = -22$$

$$b = -11$$

$$a = \dots 24 \dots$$

$$b = \dots -11 \dots$$

(3)

6. Work out the values of a and b in the identity.



$$4(2x + b) + a(x + 3) \equiv 10x + 2$$

$$8x + 4b + ax + 3a \equiv 10x + 2$$

(x)  $8 + a = 10$

$$a = 2$$

(Constants)

$$4b + 3a = 2$$

$$4b + 6 = 2$$

$$4b = -4$$

$$b = -1$$

$$a = \dots 2 \dots$$

$$b = \dots -1 \dots$$

(3)

7. Work out the values of a and b in the identity.



$$4(3x + 2) + a(x + b) \equiv 15x - 16$$

$$12x + 8 + ax + ab \equiv 15x - 16$$

(x)

$$12 + a = 15$$

$$a = 3$$

(Constants)

$$8 + ab = -16$$

$$8 + 3b = -16$$

$$3b = -24$$

$$b = -8$$

$$a = \dots\dots\dots 3$$

$$b = \dots\dots\dots -8$$

(3)

8.  $2ax + 9 - 3(x + b) \equiv 5x - 30$



Work out the values of a and b.

$$2ax + 9 - 3x - 3b \equiv 5x - 30$$

(x)

$$2a - 3 = 5$$

$$2a = 8$$

$$a = 4$$

(Constants)

$$9 - 3b = -30$$

$$-3b = -39$$

$$b = 13$$

$$a = \dots\dots\dots 4$$

$$b = \dots\dots\dots 13$$

(3)

9.

$$(x+4)(x-6) + ax + b \equiv x^2 + 8x - 25$$

Work out the values of  $a$  and  $b$ .

$$x^2 - 6x + 4x - 24 + ax + b \equiv x^2 + 8x - 25$$

$$x^2 - 2x - 24 + ax + b \equiv x^2 + 8x - 25$$

$$\boxed{x} \quad -2 + a = 8$$

$$a = 10$$

$$\boxed{\text{Constants}} \quad -24 + b = -25$$

$$b = -1$$

$$a = \dots 10 \dots$$

$$b = \dots -1 \dots$$

(3)

10.

$$(2x-5)(2x-7) + ax^2 + b \equiv 3x^2 - 24x + 12$$

Work out the values of  $a$  and  $b$ .

$$4x^2 - 14x - 10x + 35 + ax^2 + b \equiv 3x^2 - 24x + 12$$

$$4x^2 - 24x + 35 + ax^2 + b \equiv 3x^2 - 24x + 12$$

$$\boxed{x^2}$$

$$4 + a = 3$$

$$a = -1$$

$$\boxed{x}$$

$$-24 = -24 \checkmark$$

$$\boxed{\text{Constants}}$$

$$35 + b = 12$$

$$b = -23$$

$$a = \dots -1 \dots$$

$$b = \dots -23 \dots$$

(3)

11. Work out the values of a and b in the identity.



$$(x-2)^2 + x + a(x+b) \equiv x^2 + 1$$

$$(x-2)(x-2) + x + a(x+b) \equiv x^2 + 1$$

$$x^2 - 4x + 4 + x + ax + ab \equiv x^2 + 1$$

$$\boxed{x^2} \quad 1 = 1 \quad \checkmark$$

Constants

$$4 + ab = 1$$

$$4 + 3b = 1$$

$$3b = -3$$

$$b = -1$$

$$\boxed{x} \quad -4 + 1 + a = 0$$

$$-3 + a = 0$$

$$a = 3$$

$$a = \dots\dots\dots 3$$

$$b = \dots\dots\dots -1 \dots\dots\dots (3)$$

12.  $(x+b)^2 \equiv x^2 + cx + 49$



Find the two possible values of b.

$$(x+b)(x+b) \equiv x^2 + cx + 49$$

$$x^2 + 2bx + b^2 \equiv x^2 + cx + 49$$

Constants

$$b^2 = 49$$

$$b = 7 \text{ or } -7$$

$$\boxed{x} \quad 2b = c$$

$$\text{if } b=7 \quad 14=c$$

$$\text{if } b=-7 \quad -14=c$$

$$c = \dots\dots\dots 14 \quad \text{or} \quad c = \dots\dots\dots -14$$

(2)

13.

$$(x + 2c)(x + c) \equiv x^2 + dx + 50$$

Find the two possible values of  $d$ .

$$x^2 + cx + 2cx + 2c^2 \equiv x^2 + dx + 50$$

(Constants)

$$2c^2 = 50$$

$$c^2 = 25$$

$$c = 5 \text{ or } -5$$

( $x$ )

$$c + 2c = d$$

$$3c = d$$

$$\text{if } c = 5 \quad d = 15$$

$$c = -5 \quad d = -15$$

$$d = \dots 15 \dots \text{ or } d = \dots -15 \dots$$

(3)

14.

$$4x^3 + (x + a)(x + b) + cx \equiv ax^3 - 3x^3 + x^2 - x - 42$$

Work out the values of  $a$ ,  $b$  and  $c$ .

$$4x^3 + x^2 + ax + bx + ab + cx \equiv ax^3 - 3x^3 + x^2 - x - 42$$

( $x^3$ )

$$4 = a - 3$$

$$a = 7$$

(Constants)

$$ab = -42$$

$$7b = -42$$

$$b = -6$$

( $x^2$ )

$$1 = 1 \quad \checkmark$$

( $x$ )  $a + b + c = -1$

$$a = 7 \quad b = -6$$

$$a = \dots 7 \dots$$

$$7 - 6 + c = -1$$

$$b = \dots -6 \dots$$

$$1 + c = -1$$

$$c = -2$$

$$c = \dots -2 \dots$$

(5)

15.

$$(ax + 1)(x + 5)(x + b) \equiv 2x^3 + 23x^2 + 71x + 30$$



Work out the values of a and b.

$$ax \times x \times x = 2x^3$$

$$a = 2$$

$$1 \times 5 \times b = 30$$

$$b = 6$$

$$a = \dots 2 \dots$$

$$b = \dots 6 \dots$$

(2)

16.

Given that



$$(x + a)^2(x - 2) \equiv x^3 + bx^2 - 3x - 18$$

Work out the values of a and b.

$$(x^2 + 2ax + a^2)(x - 2) \equiv x^3 + bx^2 - 3x - 18$$

$$x^3 + 2ax^2 + a^2x - 2x^2 - 4ax - 2a^2 \equiv x^3 + bx^2 - 3x - 18$$

Constants

$$-2a^2 = -18$$

$$a^2 = 9$$

$$a = \pm 3$$

$x^2$

$$2a - 2 = b$$

$$6 - 2 = b$$

$$b = 4$$

$x$   $a^2 - 4a = -3$

if  $a = 3$  ~~9 - 12 = -3~~  $9 - 12 = -3$  ✓

if  $a = -3$   $9 - (-12) \neq -3$  ✗

$$a = \dots 3 \dots$$

$$b = \dots 4 \dots$$

(5)

$$\underline{\underline{a = 3}}$$

17.

Adil expands  $(x + 4)(x + c)(2x - 1)$ The coefficient of  $x^2$  is  $-9$ Find the value of  $c$ .

$$(x^2 + cx + 4x + 4c)(2x - 1)$$

$$2x^3 + \underline{2cx^2} + \underline{8x^2} + 8cx - \underline{x^2} - cx - 4x - 4c$$

$$\boxed{x^2}$$

$$2c + 8 - 1 = -9$$

$$2c + 7 = -9$$

$$2c = -16$$

$$c = -8$$

-8

.....  
(5)