

Name:

Exam Style Questions

Forming and Solving Equations



Equipment needed: Pen, calculator

Guidance

1. Read each question carefully before you begin answering it.
2. Check your answers seem right.
3. Always show your workings

Video Tutorial

www.corbettmaths.com/contents

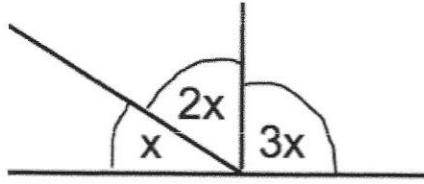
Videos 114, 115



Answers and Video Solutions



1. Three angles made up a straight line.



- (a) Form an equation in x .

$$x + 2x + 3x = 180$$

$$6x = 180$$

$$6x = 180$$

$$\underline{\hspace{10em} 6x = 180 \hspace{10em}}$$

(2)

- (b) Solve the equation to find the value of x

$$6x = 180$$

$$\div 6 \quad \div 6$$

$$x = 30$$

$$x = \underline{\hspace{10em} 30 \hspace{10em}}^\circ$$

(2)

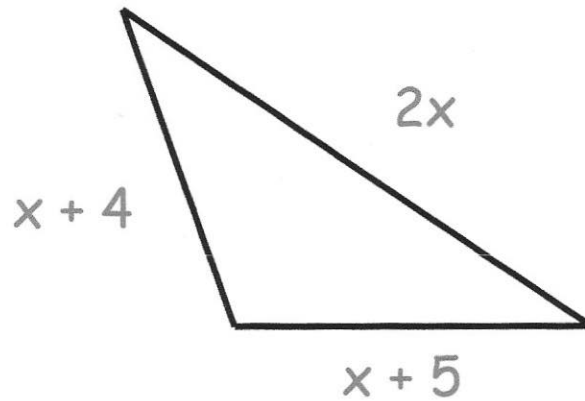
- (c) Work out the size of the largest angle.

$$30 \times 3$$

$$\underline{\hspace{10em} 90 \hspace{10em}}^\circ$$

(1)

2. The diagram below shows a triangle.
The sides are measured in centimetres.



- (a) Write an expression, in terms of x , for the perimeter of the triangle.

$$(x+4) + (x+5) + 2x$$

$$\begin{array}{r} 4x + 9 \\ \hline \end{array} \quad (2)$$

The perimeter of the triangle is 61 cm

- (b) Write down an equation in terms of x .

$$\begin{array}{r} 4x + 9 = 61 \\ \hline \end{array} \quad (1)$$

- (c) Solve the equation to find x .

$$\begin{array}{r} 4x + 9 = 61 \\ -9 \quad -9 \end{array}$$

$$4x = 52$$

$$\div 4 \quad \div 4$$

$$x = 13$$

$$\begin{array}{r} 13 \\ \hline \end{array} \quad (2)$$

3.



A child bus ticket costs £x
An adult bus ticket costs £9

Diona bought three child bus tickets and five adult bus tickets.

The total price of the bus tickets was £63 $3x$ $5 \times 9 = 45$

Find the price of a child bus ticket.

$$\begin{array}{r} 3x + 45 = 63 \\ - 45 \quad -45 \\ \hline \end{array}$$

$$3x = 18$$

$$\div 3 \quad \div 3$$

$$x = 6$$

$$\begin{array}{r} \text{£ } 6 \\ \hline \end{array} \quad (3)$$

4.



Sarah is x years old.
Thomas is 3 years older than Sarah.
David is twice as old as Sarah.
The total of their ages is 51.

(a) Write an expression for Thomas's age in terms of x.

$$\begin{array}{r} x + 3 \\ \hline \end{array} \quad (1)$$

(b) Write an expression for David's age in terms of x.

$$\begin{array}{r} 2x \\ \hline \end{array} \quad (1)$$

(c) Form an equation in x and solve it to work out Sarah's age.

$$x + (x + 3) + 2x = 51$$

$$4x + 3 = 51$$

$$\begin{array}{r} -3 \quad -3 \\ \hline \end{array}$$

$$4x = 48$$

$$\div 4 \quad \div 4$$

$$x = 12$$

$$\begin{array}{r} 12 \\ \hline \end{array} \quad (2)$$

5. James has x pence.



Hannah has 5 pence more than James. $x + 5$

Liam has 2 pence less than James. $x - 2$

The total amount of money they have is 75 pence.

(a) Use this information to write down an equation in x .

$$x + (x + 5) + (x - 2) = 75$$

$$3x + 3 = 75$$

$$3x + 3 = 75$$

.....
(2)

(b) Solve the equation to find out how much money James has.

$$3x + 3 = 75$$

$$\begin{array}{r} -3 \quad -3 \end{array}$$

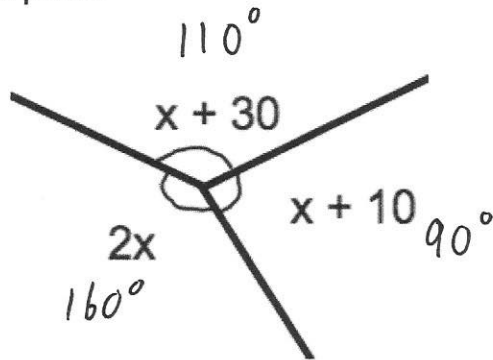
$$3x = 72$$

$$\begin{array}{r} \div 3 \quad \div 3 \end{array}$$

$$x = 24$$

.....
24 pence
(2)

6. Three angles meet at a point.



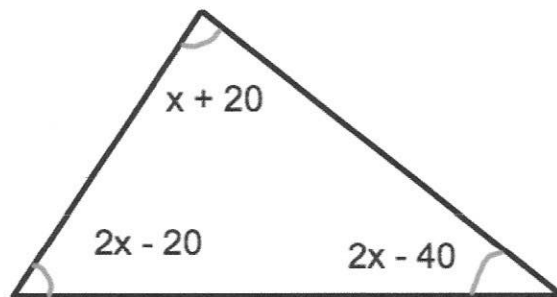
Calculate the size of the largest angle.

$$\begin{aligned}
 4x + 40 &= 360 \\
 -40 &\quad -40 \\
 4x &= 320 \\
 \div 4 &\quad \div 4 \\
 x &= 80
 \end{aligned}$$

$$\begin{array}{r}
 160 \\
 \hline
 \end{array}
 \text{ }^\circ$$

(4)

7. Shown is a triangle.



Work out the value of x .

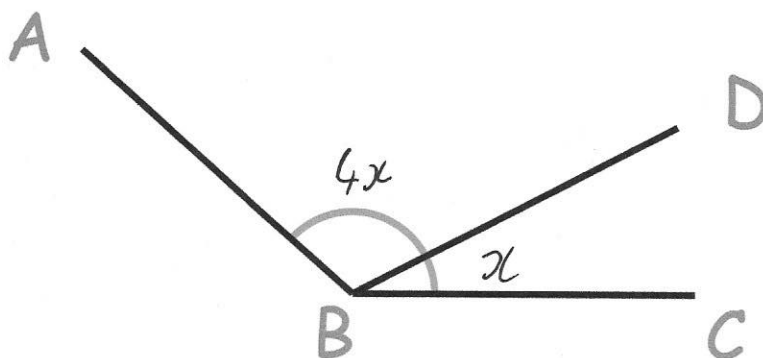
$$\begin{aligned}
 5x - 40 &= 180 \\
 +40 &\quad +40 \\
 5x &= 220 \\
 \div 5 &\quad \div 5 \\
 x &= 44
 \end{aligned}$$

$$\begin{array}{r}
 044 \\
 5 \overline{)220} \\
 \underline{220} \\
 0
 \end{array}$$

$$\begin{array}{r}
 44 \\
 x = \hline
 \end{array}
 \text{ }^\circ$$

(4)

8. ABC is an obtuse angle.



Angle ABD is four times larger than angle DBC.

$$ABC = 160^\circ$$

Work out the size of angle ABD

$$\begin{array}{r} 032 \\ 5 \overline{) 160} \end{array}$$

$$4x + x = 160$$

$$5x = 160$$

$$x = 32$$

$$\begin{array}{r} 32 \\ \times 4 \\ \hline 128 \end{array}$$

$$\begin{array}{r} 128. \\ \hline \end{array} \quad (3)$$

9. Shay recorded three songs, A, B and C.



Song B is 40 seconds longer than song A.

Song C is twice as long as song A.

The total length of the three songs is 680 seconds.

Work out the length of song B.

Give your answer in minutes and seconds.

$$\begin{aligned} \text{let Song A} &= x \\ \text{Song B} &= x + 40 \\ \text{Song C} &= 2x \end{aligned}$$

$$\begin{array}{r} 4x + 40 = 680 \\ -40 \quad -40 \\ \hline 4x = 640 \end{array}$$

$$4x = 640$$

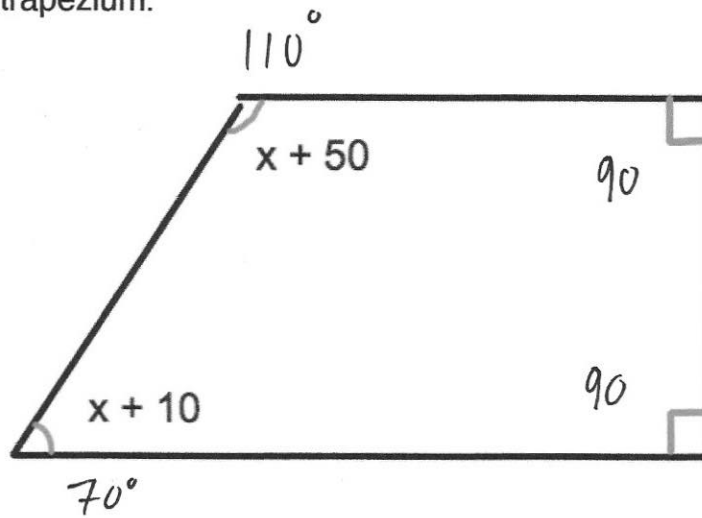
$$\div 4 \quad \div 4$$

$$x = 160$$

$$\text{Song B: } 160 + 40 = 200 \text{ seconds}$$

.....3.....minutes20.....seconds
(4)

10. Shown is a trapezium.



Calculate the size of the largest angle in the trapezium.

$$2x + 240 = 360$$
$$\begin{array}{r} -240 \\ -240 \end{array}$$

$$2x = 120$$

$$\div 2 \quad \div 2$$

$$x = 60$$

$$x = \overset{110}{\dots\dots\dots}^\circ$$

(4)

11. In a bag, there are green, yellow and blue sweets.



There are three times as many yellow sweets than blue sweets.
There are 8 less blue sweets than green sweets.

Altogether there are 128 sweets in the bag.

Work out the ratio of green sweets to blue sweets in the bag.

Let x be the number of blue sweets
 $3x$ be the number of yellow sweets
 $x+8$ be the number of green sweets.

$$\begin{array}{r} 5x + 8 = 128 \\ - 8 \quad - 8 \end{array}$$

$$\begin{array}{r} 5x = 120 \\ \div 5 \quad \div 5 \end{array}$$

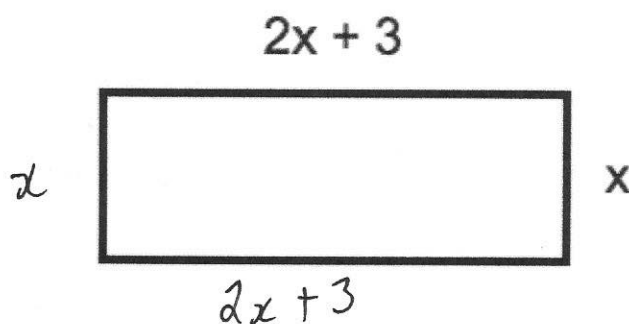
$$x = 24$$

$$\begin{array}{r} 32 : 24 \\ \div 8 \downarrow \quad \uparrow \div 8 \\ 4 : 3 \end{array}$$

24 blue sweets
32 green sweets

$$\begin{array}{r} 4 : 3 \\ \hline (5) \end{array}$$

12. Below is a rectangle, with width x cm and length $2x + 3$ cm.



The perimeter of the rectangle is 72cm.

Calculate the size of the width and length.

$$6x + 6 = 72$$

$$\begin{array}{r} -6 \quad -6 \\ \hline \end{array}$$

$$6x = 66$$

$$\div 6 \quad \div 6$$

$$x = 11$$

$$2 \times 11 = 22$$

$$22 + 3 = 25$$

$$\text{Width} = \dots\dots\dots 11 \dots\dots\dots \text{cm}$$

$$\text{Length} = \dots\dots\dots 25 \dots\dots\dots \text{cm}$$

(4)

13. The cost of a chair is £ x



A table costs £15 more than a chair. $x + 15$

The total cost of a chair and a table is £335.

Find the cost of a table.

$$x + (x + 15) = 335$$

$$\begin{array}{r} 2x + 15 = 335 \\ -15 \quad -15 \\ \hline \end{array}$$

$$2x = 320$$

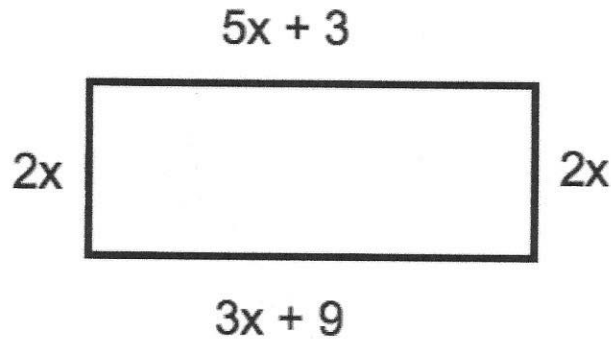
$$\div 2 \quad \div 2$$

$$x = 160$$

$$\text{£} \dots\dots\dots 175 \dots\dots\dots$$

(3)

14.



The diagram shows a rectangle. The sides are measured in centimetres.

(a) Explain why $5x + 3 = 3x + 9$

The opposite sides of a rectangle are the same length, so $5x + 3 = 3x + 9$

(1)

(b) Solve $5x + 3 = 3x + 9$

$$\begin{array}{r} -3x \quad -3x \\ 5x + 3 = 3x + 9 \end{array}$$

$$2x + 3 = 9$$

$$\begin{array}{r} -3 \quad -3 \\ 2x + 3 = 9 \end{array}$$

$$2x = 6$$

$$\begin{array}{r} \div 2 \quad \div 2 \\ 2x = 6 \end{array}$$

$$x = 3$$

$$x = \overset{3}{\dots\dots\dots} \text{cm}$$

(2)

(c) Calculate the perimeter of the rectangle.

$$5 \times 3 + 3 = 18$$

$$2 \times 3 = 6$$

$$18 + 18 + 6 + 6 = 48$$

$$\overset{48}{\dots\dots\dots} \text{cm}$$

(2)

15. Jolene buys 14 sandwiches and 9 drinks for £91 9100p
A sandwich costs 75p more than a drink.



Find the cost of a drink.

let x be the cost of a drink
 $x + 75$ is the cost of a sandwich

$$14(x + 75) + 9x = 9100 \quad x = 350$$

$$14x + 1050 + 9x = 9100$$

$$23x + 1050 = 9100$$

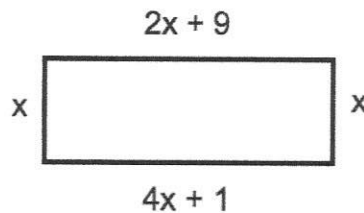
$$\begin{array}{r} -1050 \\ -1050 \end{array}$$

$$23x = 8050$$

$$\begin{array}{r} \div 23 \\ \div 23 \end{array}$$

$$\begin{array}{r} 3.50 \\ \text{£} \dots\dots\dots \\ (4) \end{array}$$

16. A rectangle is shown below.



- (a) Explain why $4x + 1 = 2x + 9$

The opposite sides of a rectangle are the same length.

(1)

- (b) Find the size of x .

$$4x + 1 = 2x + 9$$

$$\begin{array}{r} -2x \\ -2x \end{array}$$

$$2x + 1 = 9$$

$$\begin{array}{r} -1 \\ -1 \end{array}$$

$$2x = 8$$

$$x = 4$$

$$x = \begin{array}{c} 4 \\ \dots\dots\dots \end{array} \text{cm} \quad (2)$$

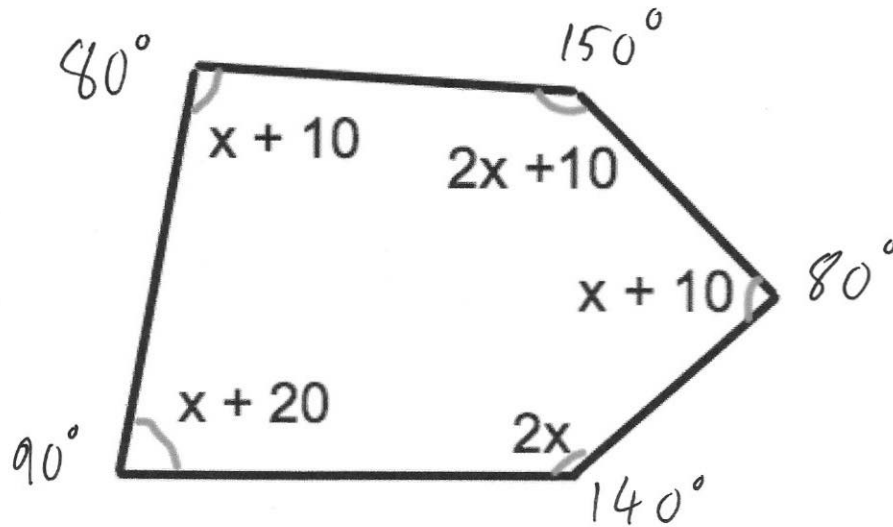
- (c) Work out the area of the rectangle.

$$4 \times 4 + 1 = 17$$

$$17 \times 4 = 68$$

$$\begin{array}{r} 68 \\ \dots\dots\dots \end{array} \text{cm}^2 \quad (2)$$

17. Shown is a pentagon, with the size of each angle shown.



Find the size of the largest angle.

$$7x + 50 = 540$$
$$\begin{array}{r} -50 \\ -50 \end{array}$$

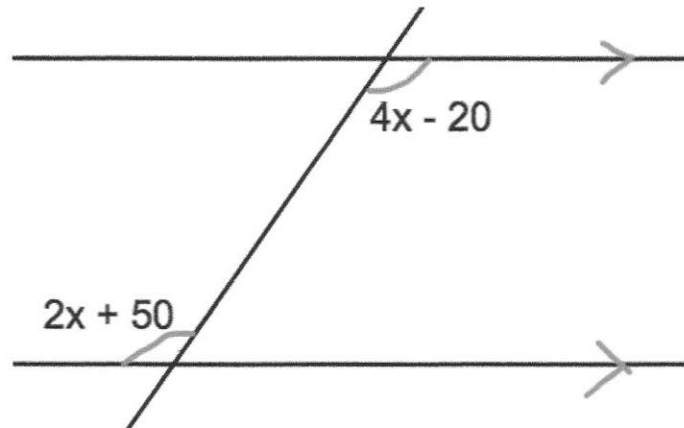
$$7x = 490$$

$$\div 7 \quad \div 7$$

$$x = 70$$

$$\begin{array}{r} 150 \\ \hline (4) \end{array}^{\circ}$$

18. The diagram below shows a pair of parallel lines.



Calculate the size of the angle, $2x + 50$.

$$\begin{array}{r} 4x - 20 = 2x + 50 \\ -2x \quad -2x \end{array}$$

$$\begin{array}{r} 2x - 20 = 50 \\ +20 \quad +20 \end{array}$$

$$2x = 70$$

$$\div 2 \quad \div 2$$

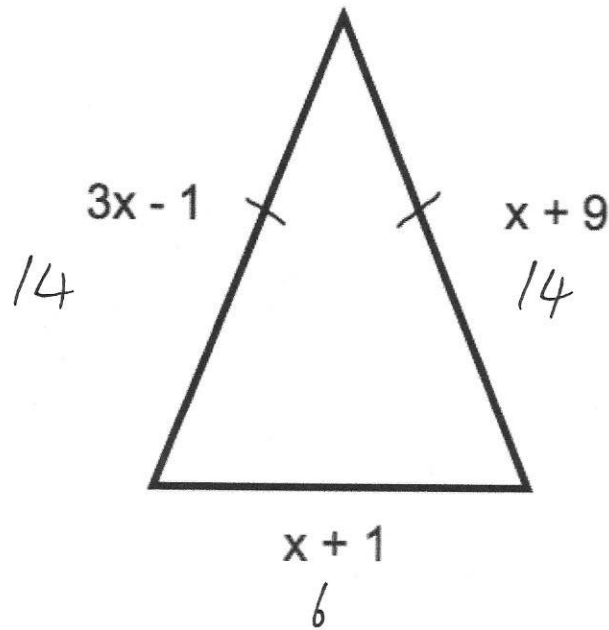
$$x = 35$$

$$2 \times 35 + 50 = 120$$

$$\begin{array}{r} 120 \\ \hline \end{array} \text{ }^\circ$$

(4)

19. Shown below is an isosceles triangle. Each side is measured in centimetres.



- (a) Explain why $3x - 1 = x + 9$

As the triangle is isosceles, the two sides that are marked as equal, are equal, so $3x - 1 = x + 9$
(1)

- (b) Solve the equation above.

$$\begin{array}{r} 3x - 1 = x + 9 \\ -x \quad -x \\ \hline 2x - 1 = 9 \\ +1 \quad +1 \\ \hline 2x = 10 \\ x = 5 \end{array}$$

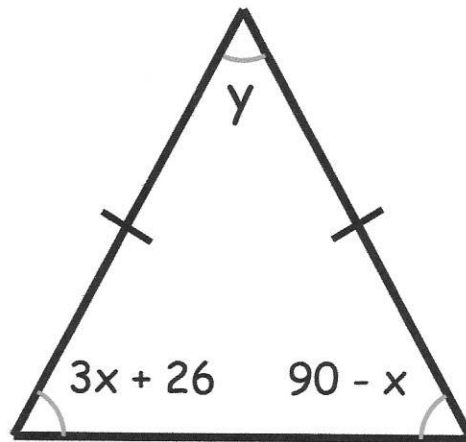
$$x = \overset{5}{\dots\dots\dots} \text{cm} \quad (2)$$

- (c) Calculate the perimeter of the triangle.

$$14 + 14 + 6 = 34$$

$$\overset{34}{\dots\dots\dots} \text{cm} \quad (2)$$

20.



Work out the size of angle y .

$$3x + 26 = 90 - x$$

$$+x$$

$$+x$$

$$4x + 26 = 90$$

$$-26 \quad -26$$

$$4x = 64$$

$$\div 4 \quad \div 4$$

$$x = 16$$

$$\begin{array}{r} 32 \\ \hline \end{array} \text{ }^\circ$$

(4)

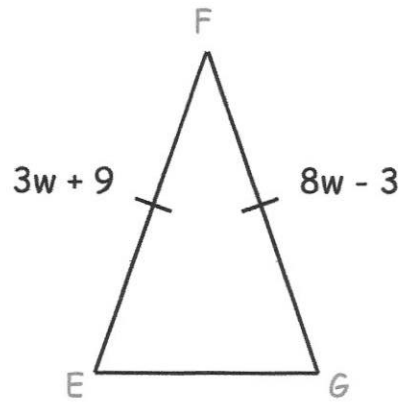
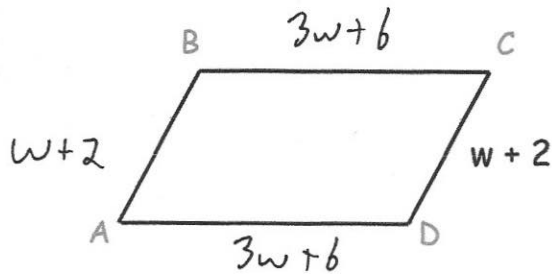
$$90 - 16 = 74$$

$$3x + 26 = 74$$

$$\begin{array}{r} + \\ \hline 148 \end{array}$$

$$180 - 148 = 32$$

21. ABCD is a parallelogram and EFG is an isosceles triangle.



$$CD = w + 2 \text{ cm}$$

$$EF = 3w + 9 \text{ cm}$$

$$FG = 8w - 3 \text{ cm}$$

$$BC = 3AB$$

The perimeter of the parallelogram is equal to the perimeter of the triangle.

Calculate the length of EG.

$$AB = w + 2$$

$$BC = 3w + 6$$

$$\begin{aligned} 3w + 9 &= 8w - 3 \\ -3w &\quad -3w \\ \hline 9 &= 5w - 3 \\ +3 &\quad +3 \\ \hline 12 &= 5w \\ \div 5 &\quad \div 5 \\ \hline w &= 2.4 \end{aligned}$$

Parallelogram:

$$\begin{aligned} (w+2) + (w+2) + (3w+6) + (3w+6) \\ = 8w + 16 \end{aligned}$$

$$8 \times 2.4 + 16 = 35.2 \text{ cm}$$

triangle:

$$3 \times 2.4 + 9 = 16.2$$

$$16.2 + 16.2 = 32.4$$

$$35.2 - 32.4 =$$

$$\dots\dots\dots 2.8 \text{ cm} \\ (5)$$

22. On Monday, Desmond ran x kilometres.



On Tuesday, he ran three kilometres less than Monday. $x - 3$

On Wednesday, Desmond ran four times the distance he ran on Monday. $4x$

The mean distance ran was 16 kilometres.

Work out how far Desmond ran on Wednesday

$$\frac{x + (x - 3) + 4x}{3} = 16$$

$$\frac{6x - 3}{3} = 16$$

$$6x - 3 = 48$$

$$6x = 51$$

$$x = 8.5$$

$$4 \times 8.5 = 34$$

34
.....km
(5)