

CANDIDATE
NAME

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CENTRE
NUMBER

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CANDIDATE
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FURTHER MATHEMATICS

9231/22

Paper 2

May/June 2017

3 hours

Candidates answer on the Question Paper.

Additional Materials: List of Formulae (MF10)

READ THESE INSTRUCTIONS FIRST

Write your Centre number, candidate number and name in the spaces at the top of this page.

Write in dark blue or black pen.

You may use an HB pencil for any diagrams or graphs.

Do not use staples, paper clips, glue or correction fluid.

DO **NOT** WRITE IN ANY BARCODES.

Answer **all** the questions.

Give non-exact numerical answers correct to 3 significant figures, or 1 decimal place in the case of angles in degrees, unless a different level of accuracy is specified in the question.

Where a numerical value is necessary, take the acceleration due to gravity to be 10 m s^{-2} .

The use of a calculator is expected, where appropriate.

Results obtained solely from a graphic calculator, without supporting working or reasoning, will not receive credit.

You are reminded of the need for clear presentation in your answers.

At the end of the examination, fasten all your work securely together.

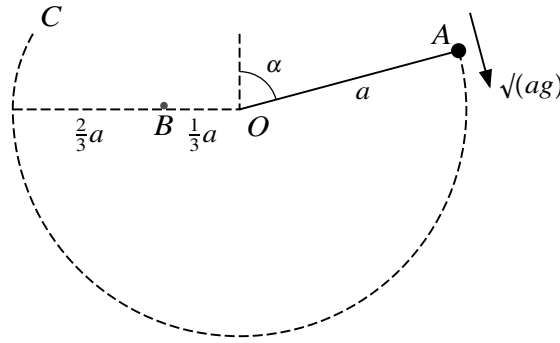
The number of marks is given in brackets [] at the end of each question or part question.

This document consists of **24** printed pages and **4** blank pages.



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5



A particle of mass m is attached to one end of a light inextensible string of length a . The other end of the string is attached to a fixed point O . The point A is such that $OA = a$ and OA makes an angle α with the upward vertical through O . The particle is held at A and then projected downwards with speed \sqrt{ag} so that it begins to move in a vertical circle with centre O . There is a small smooth peg at the point B which is at the same horizontal level as O and at a distance $\frac{1}{3}a$ from O on the opposite side of O to A (see diagram).

- (i) Show that, when the string first makes contact with the peg, the speed of the particle is $\sqrt{ag(1 + 2 \cos \alpha)}$. [2]

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The particle now begins to move in a vertical circle with centre B . When the particle is at the point C where angle $CBO = 150^\circ$, the tension in the string is the same as it was when the particle was at the point A .

- (ii) Find the value of $\cos \alpha$. [10]

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6 A fair die is thrown repeatedly until a 6 is obtained.

(i) Find the probability that obtaining a 6 takes no more than four throws. [2]

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(ii) Find the least integer N such that the probability of obtaining a 6 before the N th throw is more than 0.95. [3]

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(iii) Find the median value of Y . [3]

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(ii) Find, showing all necessary working, the value of the product moment correlation coefficient for this sample. [3]

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(iii) Test, at the 10% significance level, whether there is evidence of non-zero correlation between the variables. [4]

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11 Answer only **one** of the following two alternatives.

EITHER

A particle P of mass $3m$ is attached to one end of a light elastic spring of natural length a and modulus of elasticity kmg . The other end of the spring is attached to a fixed point O on a smooth plane that is inclined to the horizontal at an angle α , where $\sin \alpha = \frac{2}{3}$. The system rests in equilibrium with P on the plane at the point E . The length of the spring in this position is $\frac{5}{4}a$.

(i) Find the value of k . [3]

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The particle P is now replaced by a particle Q of mass $2m$ and Q is released from rest at the point E .

(ii) Show that, in the resulting motion, Q performs simple harmonic motion. State the centre and the period of the motion. [6]

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OR

A shop is supplied with large quantities of plant pots in packs of six. These pots can be damaged easily if they are not packed carefully. The manager of the shop is a statistician and he believes that the number of damaged pots in a pack of six has a binomial distribution. He chooses a random sample of 250 packs and records the numbers of damaged pots per pack. His results are shown in the following table.

Number of damaged pots per pack (x)	0	1	2	3	4	5	6
Frequency	48	69	78	32	22	1	0

(i) Show that the mean number of damaged pots per pack in this sample is 1.656. [1]

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The following table shows some of the expected frequencies, correct to 2 decimal places, using an appropriate binomial distribution.

Number of damaged pots per pack (x)	0	1	2	3	4	5	6
Expected frequency	36.01	82.36	a	39.89	b	1.74	0.11

(ii) Find the values of a and b , correct to 2 decimal places [5]

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